

## Department of Mathematics Faculty of Sciences, Jamia Millia Islamia

## B. Sc. (Hons.) Mathematics Course Structure and Syllabus (w. e. f. 2024-25)

Semester -	– III		
Category	Code	Title of Paper	Credits
Major	24MATC201	Real Analysis	4
Major	24MATC202	Group Theory	4
		Total Credits	8

## 24MATC201 Real Analysis

- Unit-I Bounded and unbounded sets, Infimum, supremum of a set and properties, Order completeness property of R, Archimedian property of R, Neighbourhoods, Open sets, Interior points, limit points of a set, Closed sets and related results. Derived sets, Closure of a set, Bolzano-Weierstrass theorem for sets
- Unit-II Sequence of real numbers, Bounded sequences, Convergent and divergent sequences, Subsequences, limit points of a sequence, Bolzano Weierstrass theorem for sequences, Limit inferior and limit superior, Algebra of sequences, Monotone sequences, Monotone Convergence Theorem, Cauchy's sequence, Cauchy's general principal of convergence, Cauchy's first & second theorems on limits of sequences
- Unit-III Infinite series: convergence and divergence, Cauchy's criterion for convergence of a series, Test for convergence of positive term series, Comparison tests, Ratio test, Cauchy's nth root test, Raabe's test, Alternating series, Leibnitz test, Absolute and conditional convergence
- Unit-IV Continuous functions:  $\epsilon \delta$  approach, Sequential criterion for continuity, Theorems on continuity, Uniform continuity, Relation between continuity and uniform continuity, Derivative, Increasing and decreasing functions, Darboux theorem.

Books Recommended

- 1. R. G. Bartle and D. R. Sherbeer Introduction to Real Analysis (3rd Edition), John Wiley and Sons (Asia) Pvt. Ltd., Singapore, 2003
- 2. S. C. Malik and S. Arora Mathematical Analysis, New Age International (P) Ltd. Publishers, 2009
- S. R. Ghorpade and B. V. Limaye: A course in Calculus and Real Analysis, Undergraduate Text in Maths. Springer (SIE), Indian reprint 2006
- 4. T. M. Apostol: Mathematica. Analysis, Addison-Wesley Series in Mathematics, 1974

24MATC202	Group Theory
Unit-I	Sets, Relations, Functions, and binary operations (Review), Groups with examples and their
	properties, Subgroups, Cosets, Lagrange's theorem and its consequences, Order of an
	element of a group, Cyclic groups, Normal subgroups, Factor groups.
Unit-II	Group homomorphism, Kernel of a homomorphism, The homomorphism theorems,
	Isomorphisms, The isomorphism theorems, Permutation groups, Even and odd permutations,
	Alternating groups, Cayley's theorem, and regular permutation group.
Unit-III	Automorphism, Inner automorphism, Automorphism group of finite and infinite cyclic
	groups, Conjugacy relation, Normalizer and Centre, External direct products, and internal
	direct products.
Unit-IV	Class equation of a finite group and its applications, Structure of finite Abelian groups,
	Cauchy's theorem, Sylow's theorems and its consequences, Simple groups, and non-
	simplicity tests.
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## Books Recommended

- 1. Surjeet Singh and Q. Zameeruddin: Modern Algebra, Vikas Publ. House, New Delhi, 2002.
- 2. I.N.Herstein, Topics in Algebra, John Wiley & Sons, New York, 2006.
- 3. J. A. Gallian, Contemporary Abstract Algebra, Narosa Publishing House, New Delhi, 1998.
- 4. N. S. Gopalakrishan: University Algebra, New Age Int. Publishers, New Delhi, 2015.
- 5. N. Jacobson: Basic Algebra Vol. I & II, W. H. Freeman and Company, New York 1974.
- 6. J. B. Fraleigh, A first Course in Abstract Algebra, Pearson Education Inc. Essex, 2002.